

Q. 1 – Q. 25 carry one mark each.

Q.1 Consider a system of linear equations:

$$x - 2y + 3z = -1,$$

$$x - 3y + 4z = 1, \text{ and}$$

$$-2x + 4y - 6z = k.$$

The value of k for which the system has infinitely many solutions is _____.

Q.2 A function $f(x) = 1 - x^2 + x^3$ is defined in the closed interval $[-1, 1]$. The value of x , in the open interval $(-1, 1)$ for which the mean value theorem is satisfied, is

(A) $-1/2$

(B) $-1/3$

(C) $1/3$

(D) $1/2$

Q.3 Suppose A and B are two independent events with probabilities $P(A) \neq 0$ and $P(B) \neq 0$. Let $\bar{A}$ and $\bar{B}$ be their complements. Which one of the following statements is FALSE?

(A) $P(A \cap B) = P(A)P(B)$

(B) $P(A|B) = P(A)$

(C) $P(A \cup B) = P(A) + P(B)$

(D) $P(\bar{A} \cap \bar{B}) = P(\bar{A})P(\bar{B})$

Q.4 Let $z = x + iy$ be a complex variable. Consider that contour integration is performed along the unit circle in anticlockwise direction. Which one of the following statements is **NOT TRUE**?

(A) The residue of $\frac{z}{z^2 - 1}$ at $z = 1$ is $1/2$

(B) $\oint_C z^2 dz = 0$

(C) $\frac{1}{2\pi i} \oint_C \frac{1}{z} dz = 1$

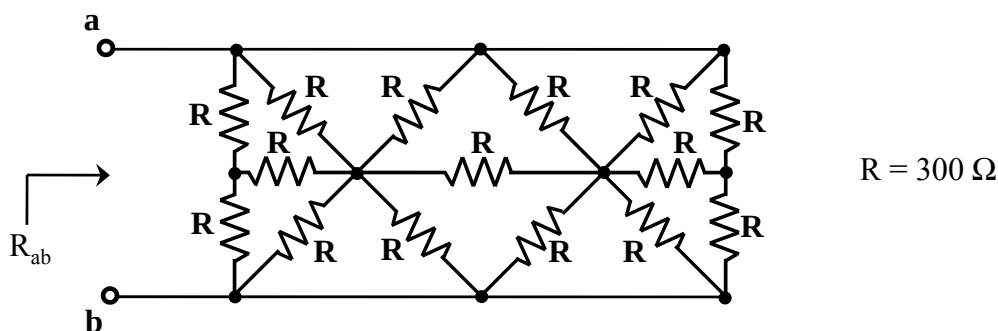
(D) $\bar{z}$ (complex conjugate of z) is an analytical function

Q.5 The value of p such that the vector $\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$ is an eigenvector of the matrix $\begin{bmatrix} 4 & 1 & 2 \\ p & 2 & 1 \\ 14 & -4 & 10 \end{bmatrix}$ is _____.

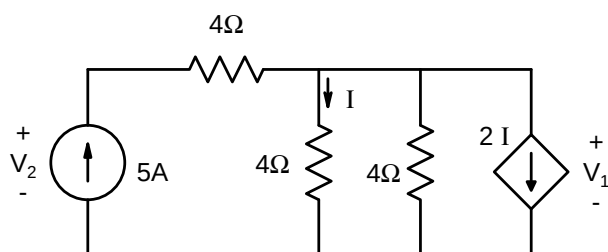
Q.6 In the circuit shown, at resonance, the amplitude of the sinusoidal voltage (in Volts) across the capacitor is _____.



- Q.7 In the network shown in the figure, all resistors are identical with $R = 300 \Omega$. The resistance R_{ab} (in Ω) of the network is _____.

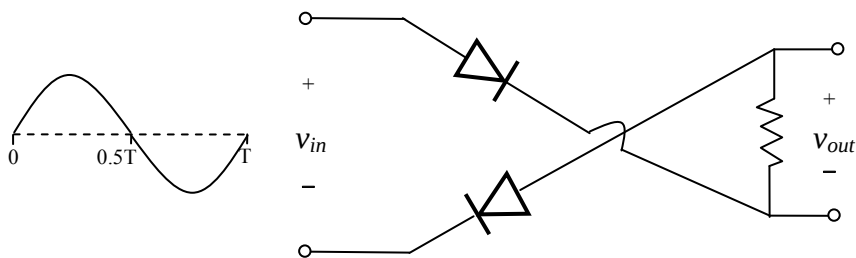


- Q.8 In the given circuit, the values of V_1 and V_2 respectively are



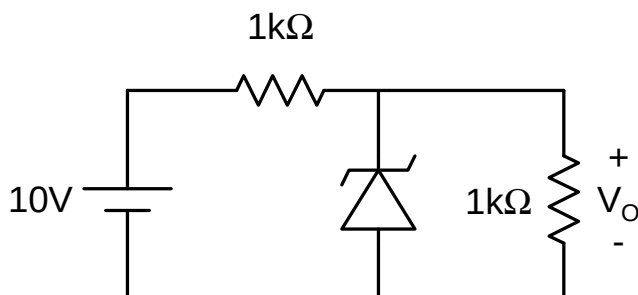
- (A) 5 V, 25 V (B) 10 V, 30 V (C) 15 V, 35 V (D) 0 V, 20 V
- Q.9 A region of negative differential resistance is observed in the current voltage characteristics of a silicon PN junction if
- (A) both the P-region and the N-region are heavily doped
 (B) the N-region is heavily doped compared to the P-region
 (C) the P-region is heavily doped compared to the N-region
 (D) an intrinsic silicon region is inserted between the P-region and the N-region
- Q.10 A silicon sample is uniformly doped with donor type impurities with a concentration of $10^{16} / \text{cm}^3$. The electron and hole mobilities in the sample are $1200 \text{ cm}^2/\text{V-s}$ and $400 \text{ cm}^2/\text{V-s}$ respectively. Assume complete ionization of impurities. The charge of an electron is $1.6 \times 10^{-19} \text{ C}$. The resistivity of the sample (in $\Omega\text{-cm}$) is _____.

- Q.11 For the circuit with ideal diodes shown in the figure, the shape of the output (v_{out}) for the given sine wave input (v_{in}) will be

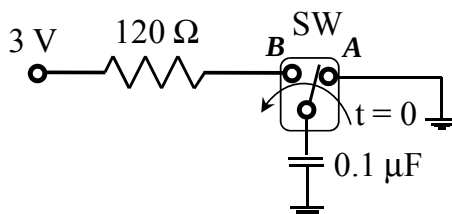


- (A)
- (B)
- (C)
- (D)

- Q.12 In the circuit shown below, the Zener diode is ideal and the Zener voltage is 6 V. The output voltage V_o (in volts) is _____.

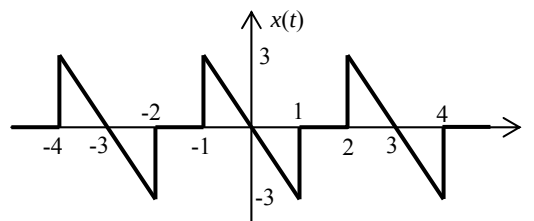


- Q.13 In the circuit shown, the switch SW is thrown from position A to position B at time $t = 0$. The energy (in μJ) taken from the 3 V source to charge the $0.1 \mu\text{F}$ capacitor from 0 V to 3 V is



- (A) 0.3 (B) 0.45 (C) 0.9 (D) 3

- Q.14 In an 8085 microprocessor, the shift registers which store the result of an addition and the overflow bit are, respectively
- (A) B and F
(B) A and F
(C) H and F
(D) A and C
- Q.15 A 16 Kb (=16,384 bit) memory array is designed as a square with an aspect ratio of one (number of rows is equal to the number of columns). The minimum number of address lines needed for the row decoder is _____.
- Q.16 Consider a four bit D to A converter. The analog value corresponding to digital signals of values 0000 and 0001 are 0 V and 0.0625 V respectively. The analog value (in Volts) corresponding to the digital signal 1111 is _____.
- Q.17 The result of the convolution $x(-t) * \delta(-t - t_0)$ is
- (A) $x(t + t_0)$ (B) $x(t - t_0)$ (C) $x(-t + t_0)$ (D) $x(-t - t_0)$
- Q.18 The waveform of a periodic signal $x(t)$ is shown in the figure.



A signal $g(t)$ is defined by $g(t) = x\left(\frac{t-1}{2}\right)$. The average power of $g(t)$ is _____.

- Q.19 Negative feedback in a closed-loop control system **DOES NOT**
- (A) reduce the overall gain (B) reduce bandwidth
(C) improve disturbance rejection (D) reduce sensitivity to parameter variation
- Q.20 A unity negative feedback system has the open-loop transfer function $G(s) = \frac{K}{s(s+1)(s+3)}$. The value of the gain K (>0) at which the root locus crosses the imaginary axis is _____.
- Q.21 The polar plot of the transfer function $G(s) = \frac{10(s+1)}{s+10}$ for $0 \leq \omega < \infty$ will be in the
- (A) first quadrant
(B) second quadrant
(C) third quadrant
(D) fourth quadrant

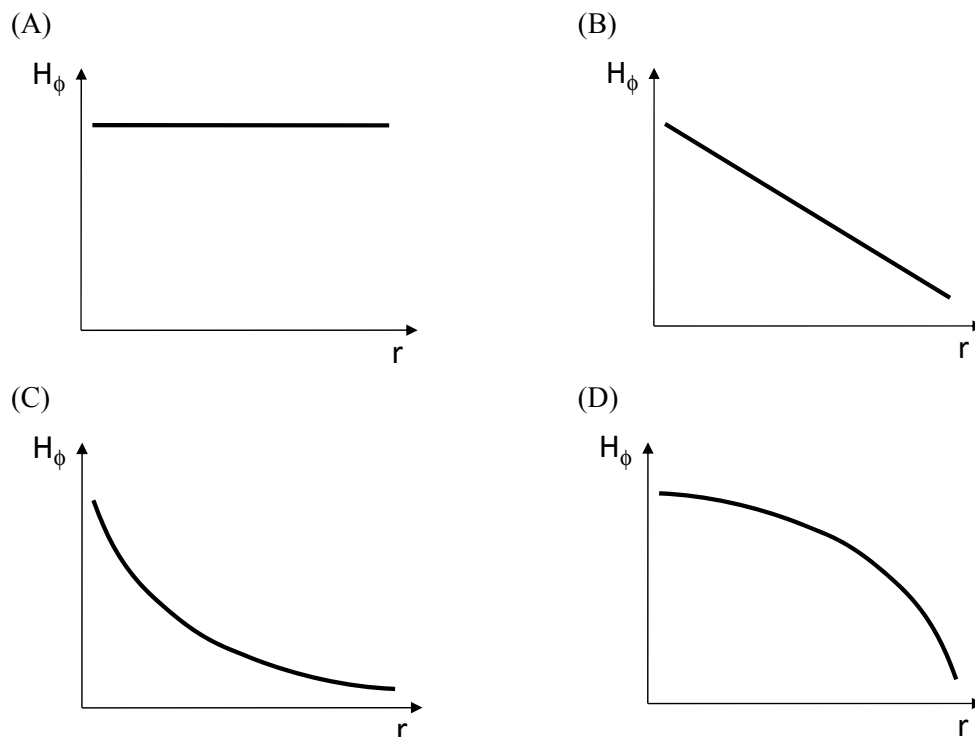
Q.22 A sinusoidal signal of 2 kHz frequency is applied to a delta modulator. The sampling rate and step-size Δ of the delta modulator are 20,000 samples per second and 0.1 V, respectively. To prevent slope overload, the maximum amplitude of the sinusoidal signal (in Volts) is

- (A) $\frac{1}{2\pi}$ (B) $\frac{1}{\pi}$
 (C) $\frac{2}{\pi}$ (D) π

Q.23 Consider the signal $s(t) = m(t)\cos(2\pi f_c t) + \hat{m}(t)\sin(2\pi f_c t)$ where $\hat{m}(t)$ denotes the Hilbert transform of $m(t)$ and the bandwidth of $m(t)$ is very small compared to f_c . The signal $s(t)$ is a

- (A) high-pass signal
 (B) low-pass signal
 (C) band-pass signal
 (D) double sideband suppressed carrier signal

Q.24 Consider a straight, infinitely long, current carrying conductor lying on the z-axis. Which one of the following plots (in linear scale) qualitatively represents the dependence of H_ϕ on r , where H_ϕ is the magnitude of the azimuthal component of magnetic field outside the conductor and r is the radial distance from the conductor?



Q.25 The electric field component of a plane wave traveling in a lossless dielectric medium is given by

$$\vec{E}(z, t) = \hat{a}_y 2 \cos\left(10^8 t - \frac{z}{\sqrt{2}}\right) \text{ V/m. The wavelength (in m) for the wave is } \underline{\hspace{2cm}}.$$

Q. 26 – Q. 55 carry two marks each.

Q.26

The solution of the differential equation $\frac{d^2y}{dt^2} + 2\frac{dy}{dt} + y = 0$ with $y(0) = y'(0) = 1$ is

(A) $(2-t)e^t$

(B) $(1+2t)e^{-t}$

(C) $(2+t)e^{-t}$

(D) $(1-2t)e^t$

Q.27

A vector $\vec{P}$ is given by $\vec{P} = x^3y \vec{a}_x - x^2y^2 \vec{a}_y - x^2yz \vec{a}_z$. Which one of the following statements is **TRUE**?

(A) $\vec{P}$ is solenoidal, but not irrotational

(B) $\vec{P}$ is irrotational, but not solenoidal

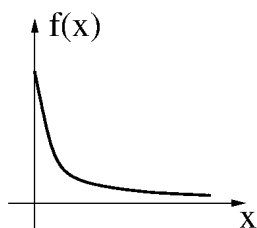
(C) $\vec{P}$ is neither solenoidal nor irrotational

(D) $\vec{P}$ is both solenoidal and irrotational

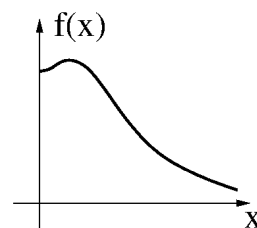
Q.28

Which one of the following graphs describes the function $f(x) = e^{-x}(x^2 + x + 1)$?

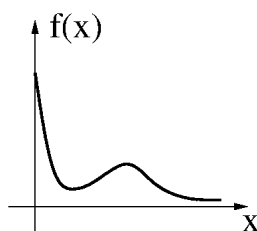
(A)



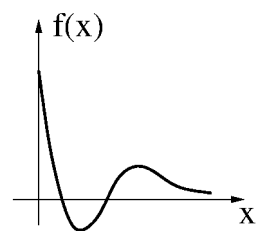
(B)



(C)



(D)



Q.29

The maximum area (in square units) of a rectangle whose vertices lie on the ellipse $x^2 + 4y^2 = 1$ is _____.

Q.30

The damping ratio of a series RLC circuit can be expressed as

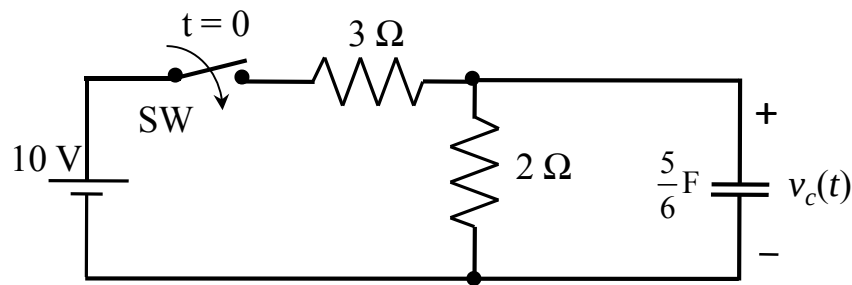
(A) $\frac{R^2C}{2L}$

(B) $\frac{2L}{R^2C}$

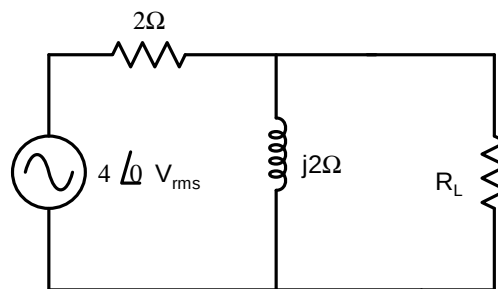
(C) $\frac{R}{2} \sqrt{\frac{C}{L}}$

(D) $\frac{2}{R} \sqrt{\frac{L}{C}}$

- Q.31 In the circuit shown, switch SW is closed at $t = 0$. Assuming zero initial conditions, the value of $v_c(t)$ (in Volts) at $t = 1$ sec is _____.

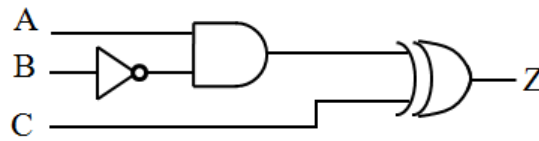


- Q.32 In the given circuit, the maximum power (in Watts) that can be transferred to the load R_L is _____.



- Q.33 The built-in potential of an abrupt p-n junction is 0.75 V. If its junction capacitance (C_J) at a reverse bias (V_R) of 1.25 V is 5 pF, the value of C_J (in pF) when $V_R = 7.25$ V is _____.
- Q.34 A MOSFET in saturation has a drain current of 1 mA for $V_{DS} = 0.5$ V. If the channel length modulation coefficient is 0.05 V^{-1} , the output resistance (in $\text{k}\Omega$) of the MOSFET is _____.
- Q.35 For a silicon diode with long P and N regions, the acceptor and donor impurity concentrations are $1 \times 10^{17} \text{ cm}^{-3}$ and $1 \times 10^{15} \text{ cm}^{-3}$, respectively. The lifetimes of electrons in P region and holes in N region are both 100 μs . The electron and hole diffusion coefficients are 49 cm^2/s and 36 cm^2/s , respectively. Assume $kT/q = 26 \text{ mV}$, the intrinsic carrier concentration is $1 \times 10^{10} \text{ cm}^{-3}$, and $q = 1.6 \times 10^{-19} \text{ C}$. When a forward voltage of 208 mV is applied across the diode, the hole current density (in nA/cm^2) injected from P region to N region is _____.
- Q.36 The Boolean expression $F(X,Y,Z) = \bar{X}Y\bar{Z} + X\bar{Y}\bar{Z} + XY\bar{Z} + XYZ$ converted into the canonical product of sum (POS) form is
- (A) $(X+Y+Z)(X+Y+\bar{Z})(X+\bar{Y}+\bar{Z})(\bar{X}+Y+\bar{Z})$ (B) $(X+\bar{Y}+Z)(\bar{X}+Y+\bar{Z})(\bar{X}+\bar{Y}+Z)(\bar{X}+\bar{Y}+\bar{Z})$
- (C) $(X+Y+Z)(\bar{X}+Y+\bar{Z})(X+\bar{Y}+Z)(\bar{X}+\bar{Y}+\bar{Z})$ (D) $(X+\bar{Y}+\bar{Z})(\bar{X}+Y+Z)(\bar{X}+\bar{Y}+Z)(X+Y+Z)$

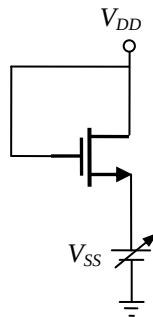
- Q.37 All the logic gates shown in the figure have a propagation delay of 20 ns. Let $A = C = 0$ and $B = 1$ until time $t = 0$. At $t = 0$, all the inputs flip (i.e., $A = C = 1$ and $B = 0$) and remain in that state. For $t > 0$, output $Z = 1$ for a duration (in ns) of _____.



- Q.38 A 3-input majority gate is defined by the logic function $M(a, b, c) = ab + bc + ca$. Which one of the following gates is represented by the function $M(M(a, b, c), M(a, b, \bar{c}), c)$?

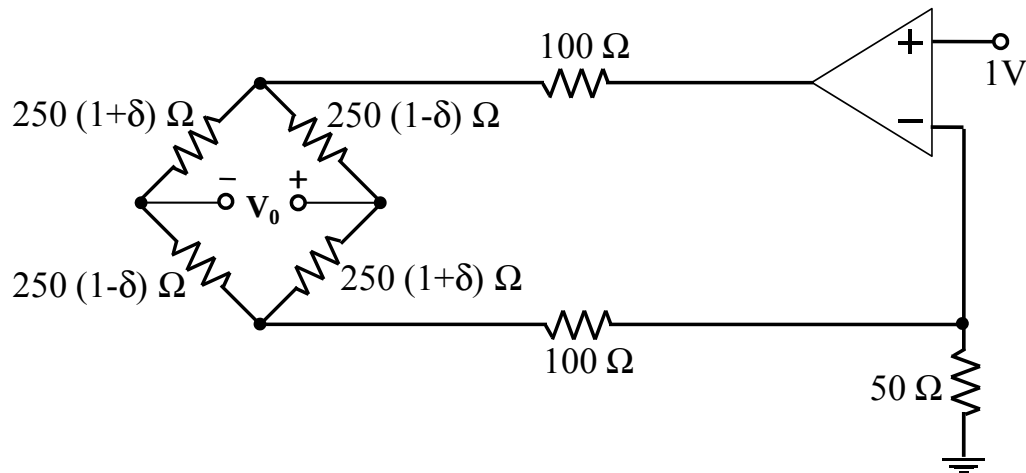
- (A) 3-input NAND gate (B) 3-input XOR gate
(C) 3-input NOR gate (D) 3-input XNOR gate

- Q.39 For the NMOSFET in the circuit shown, the threshold voltage is V_{th} , where $V_{th} > 0$. The source voltage V_{SS} is varied from 0 to V_{DD} . Neglecting the channel length modulation, the drain current I_D as a function of V_{SS} is represented by

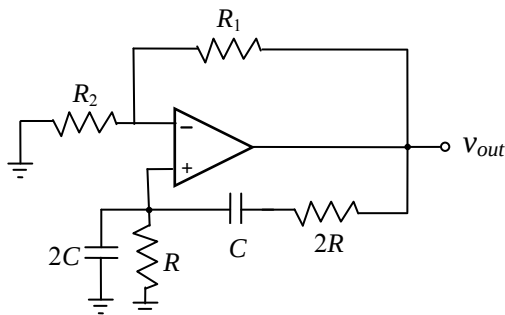


- (A) (B)
- (C) (D)

- Q.40 In the circuit shown, assume that the opamp is ideal. The bridge output voltage V_0 (in mV) for $\delta = 0.05$ is _____.

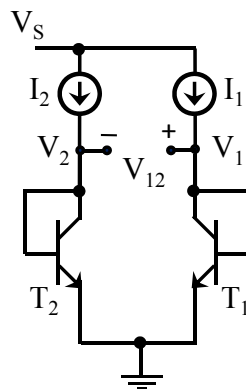


- Q.41 The circuit shown in the figure has an ideal opamp. The oscillation frequency and the condition to sustain the oscillations, respectively, are



- (A) $\frac{1}{CR}$ and $R_1 = R_2$ (B) $\frac{1}{CR}$ and $R_1 = 4R_2$
 (C) $\frac{1}{2CR}$ and $R_1 = R_2$ (D) $\frac{1}{2CR}$ and $R_1 = 4R_2$

- Q.42 In the circuit shown, $I_1 = 80$ mA and $I_2 = 4$ mA. Transistors T_1 and T_2 are identical. Assume that the thermal voltage V_T is 26 mV at 27 °C. At 50 °C, the value of the voltage $V_{12} = V_1 - V_2$ (in mV) is _____.



Q.43 Two sequences $[a, b, c]$ and $[A, B, C]$ are related as,

$$\begin{bmatrix} A \\ B \\ C \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & W_3^{-1} & W_3^{-2} \\ 1 & W_3^{-2} & W_3^{-4} \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} \quad \text{where } W_3 = e^{j\frac{2\pi}{3}}.$$

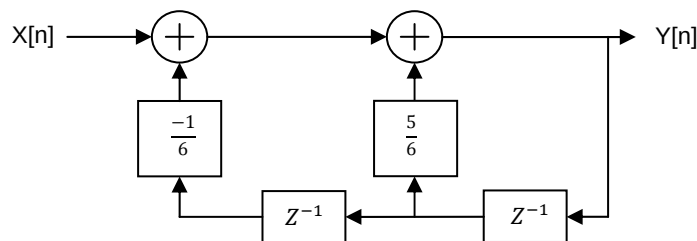
If another sequence $[p, q, r]$ is derived as,

$$\begin{bmatrix} p \\ q \\ r \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & W_3^1 & W_3^2 \\ 1 & W_3^2 & W_3^4 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & W_3^2 & 0 \\ 0 & 0 & W_3^4 \end{bmatrix} \begin{bmatrix} A/3 \\ B/3 \\ C/3 \end{bmatrix},$$

then the relationship between the sequences $[p, q, r]$ and $[a, b, c]$ is

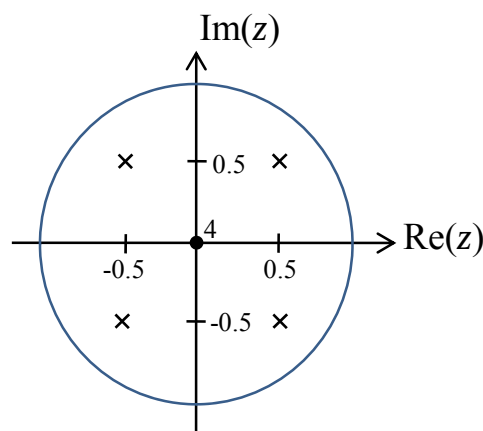
- (A) $[p, q, r] = [b, a, c]$ (B) $[p, q, r] = [b, c, a]$
 (C) $[p, q, r] = [c, a, b]$ (D) $[p, q, r] = [c, b, a]$

Q.44 For the discrete-time system shown in the figure, the poles of the system transfer function are located at



- (A) 2, 3 (B) $\frac{1}{2}, 3$ (C) $\frac{1}{2}, \frac{1}{3}$ (D) 2, $\frac{1}{3}$

Q.45 The pole-zero diagram of a causal and stable discrete-time system is shown in the figure. The zero at the origin has multiplicity 4. The impulse response of the system is $h[n]$. If $h[0] = 1$, we can conclude



- (A) $h[n]$ is real for all n
 (B) $h[n]$ is purely imaginary for all n
 (C) $h[n]$ is real for only even n
 (D) $h[n]$ is purely imaginary for only odd n

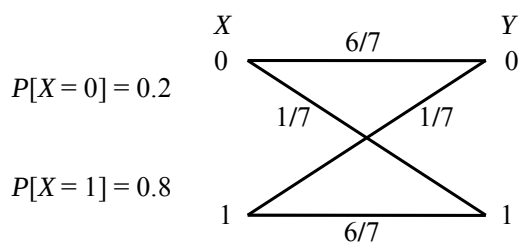
Q.46 The open-loop transfer function of a plant in a unity feedback configuration is given as $G(s) = \frac{K(s+4)}{(s+8)(s^2-9)}$. The value of the gain $K(>0)$ for which $-1 + j2$ lies on the root locus is _____.

Q.47 A lead compensator network includes a parallel combination of R and C in the feed-forward path. If the transfer function of the compensator is $G_c(s) = \frac{s+2}{s+4}$, the value of RC is _____.

Q.48 A plant transfer function is given as $G(s) = \left(K_p + \frac{K_I}{s}\right) \frac{1}{s(s+2)}$. When the plant operates in a unity feedback configuration, the condition for the stability of the closed loop system is

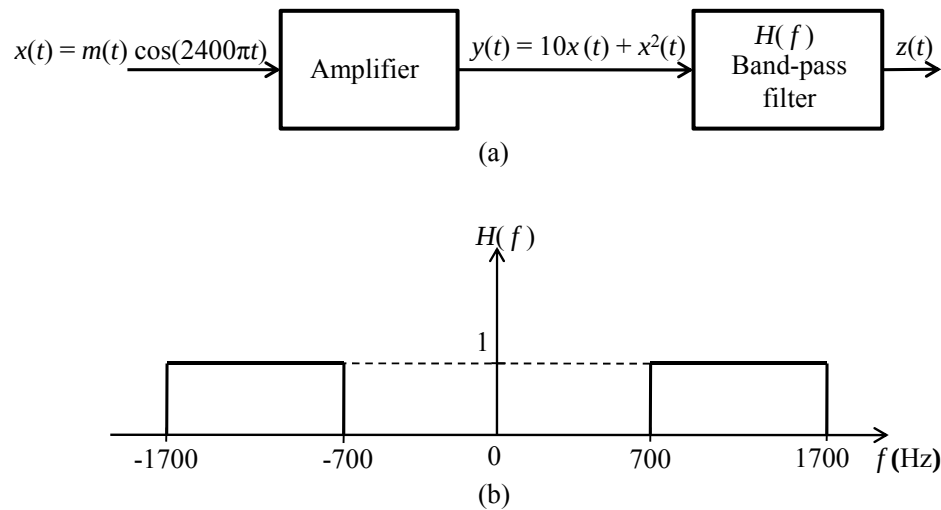
- (A) $K_p > \frac{K_I}{2} > 0$ (B) $2K_I > K_p > 0$ (C) $2K_I < K_p$ (D) $2K_I > K_p$

Q.49 The input X to the Binary Symmetric Channel (BSC) shown in the figure is '1' with probability 0.8. The cross-over probability is $1/7$. If the received bit $Y = 0$, the conditional probability that '1' was transmitted is _____.



Q.50 The transmitted signal in a GSM system is of 200 kHz bandwidth and 8 users share a common bandwidth using TDMA. If at a given time 12 users are talking in a cell, the total bandwidth of the signal received by the base station of the cell will be at least (in kHz) _____.

- Q.51 In the system shown in Figure (a), $m(t)$ is a low-pass signal with bandwidth W Hz. The frequency response of the band-pass filter $H(f)$ is shown in Figure (b). If it is desired that the output signal $z(t) = 10x(t)$, the maximum value of W (in Hz) should be strictly less than _____.



- Q.52 A source emits bit 0 with probability $\frac{1}{3}$ and bit 1 with probability $\frac{2}{3}$. The emitted bits are communicated to the receiver. The receiver decides for either 0 or 1 based on the received value R . It is given that the conditional density functions of R are as

$$f_{R|0}(r) = \begin{cases} \frac{1}{4}, & -3 \leq x \leq 1, \\ 0, & \text{otherwise,} \end{cases} \quad \text{and} \quad f_{R|1}(r) = \begin{cases} \frac{1}{6}, & -1 \leq x \leq 5, \\ 0, & \text{otherwise.} \end{cases}$$

The minimum decision error probability is

- (A) 0 (B) 1/12 (C) 1/9 (D) 1/6
- Q.53 The longitudinal component of the magnetic field inside an air-filled rectangular waveguide made of a perfect electric conductor is given by the following expression

$$H_z(x, y, z, t) = 0.1 \cos(25\pi x) \cos(30.3\pi y) \cos(12\pi \times 10^9 t - \beta z) \quad (\text{A/m})$$

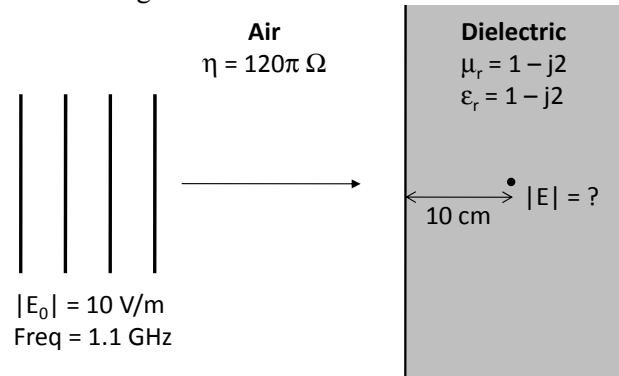
The cross-sectional dimensions of the waveguide are given as $a = 0.08$ m and $b = 0.033$ m. The mode of propagation inside the waveguide is

- (A) TM_{12} (B) TM_{21}
 (C) TE_{21} (D) TE_{12}
- Q.54 The electric field intensity of a plane wave traveling in free space is given by the following expression

$$\mathbf{E}(x, t) = \mathbf{a}_y 24\pi \cos(\omega t - k_0 x) \quad (\text{V/m})$$

In this field, consider a square area 10 cm x 10 cm on a plane $x + y = 1$. The total time-average power (in mW) passing through the square area is _____.

- Q.55 Consider a uniform plane wave with amplitude (E_0) of 10 V/m and 1.1 GHz frequency travelling in air, and incident normally on a dielectric medium with complex relative permittivity (ϵ_r) and permeability (μ_r) as shown in the figure.



The magnitude of the transmitted electric field component (in V/m) after it has travelled a distance of 10 cm inside the dielectric region is _____.

END OF THE QUESTION PAPER

Graduate Aptitude Test in Engineering

Notations :

- Options shown in green color and with ✓ icon are correct.
- Options shown in red color and with ✗ icon are incorrect.

Question Paper Name: EC: ELECTRONICS AND COMMUNICATION ENGINEERING 31st Jan Shift1
Number of Questions: 65
Total Marks: 100.0

Wrong answer for MCQ will result in negative marks, (-1/3) for 1 mark Questions and (-2/3) for 2 marks Questions.

General Aptitude

Number of Questions: 10
Section Marks: 15.0

Q.1 to Q.5 carry 1 mark each & Q.6 to Q.10 carry 2 marks each.

Question Number : 1 Question Type : MCQ

Choose the most appropriate word from the options given below to complete the following sentence.

The principal presented the chief guest with a _____, as token of appreciation.

- (A) momento (B) memento (C) momentum (D) moment

Options :

- ✗ A
- ✓ B
- ✗ C
- ✗ D

Question Number : 2 Question Type : MCQ

Choose the appropriate word/phrase, out of the four options given below, to complete the following sentence:

Frogs _____.

- (A) croak (B) roar (C) hiss (D) patter

Options :

- ✓ A
- ✗ B
- ✗ C
- ✗ D

Question Number : 3 Question Type : MCQ



Choose the word most similar in meaning to the given word:

Educe

- (A) Exert (B) Educate (C) Extract (D) Extend

Options :

1. ✗ A
2. ✗ B
3. ✓ C
4. ✗ D

Question Number : 4 Question Type : MCQ

Operators $\square$, $\diamond$ and $\rightarrow$ are defined by: $a \square b = \frac{a-b}{a+b}$; $a \diamond b = \frac{a+b}{a-b}$; $a \rightarrow b = ab$.

Find the value of $(66 \square 6) \rightarrow (66 \diamond 6)$.

- (A) -2 (B) -1 (C) 1 (D) 2

Options :

1. ✗ A
2. ✗ B
3. ✓ C
4. ✗ D

Question Number : 5 Question Type : MCQ

If $\log_x (5/7) = -1/3$, then the value of x is

- (A) 343/125
(B) 125/343
(C) -25/49
(D) -49/25

Options :

1. ✓ A
2. ✗ B
3. ✗ C
4. ✗ D

Question Number : 6 Question Type : MCQ

The following question presents a sentence, part of which is underlined. Beneath the sentence you find four ways of phrasing the underlined part. Following the requirements of the standard written English, select the answer that produces the most effective sentence.

Tuberculosis, together with its effects, ranks one of the leading causes of death in India.

- (A) ranks as one of the leading causes of death
(B) rank as one of the leading causes of death
(C) has the rank of one of the leading causes of death
(D) are one of the leading causes of death



Options :

1. ✓ A
2. ✗ B
3. ✗ C
4. ✗ D

Question Number : 7 Question Type : MCQ

Read the following paragraph and choose the correct statement.

Climate change has reduced human security and threatened human well being. An ignored reality of human progress is that human security largely depends upon environmental security. But on the contrary, human progress seems contradictory to environmental security. To keep up both at the required level is a challenge to be addressed by one and all. One of the ways to curb the climate change may be suitable scientific innovations, while the other may be the Gandhian perspective on small scale progress with focus on sustainability.

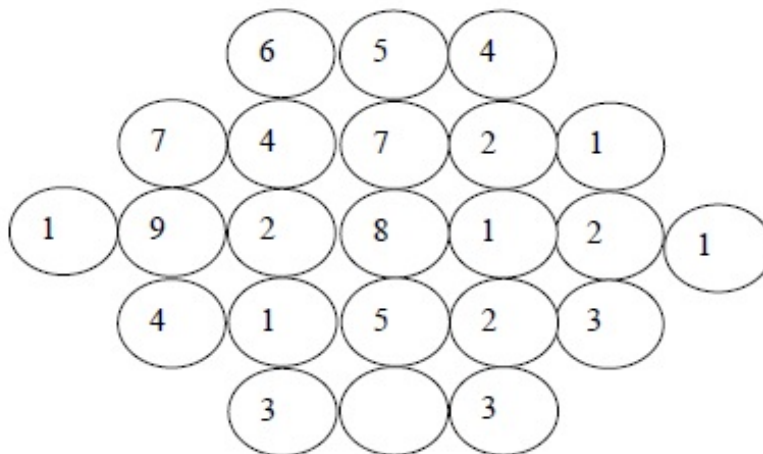
- (A) Human progress and security are positively associated with environmental security.
- (B) Human progress is contradictory to environmental security.
- (C) Human security is contradictory to environmental security.
- (D) Human progress depends upon environmental security.

Options :

1. ✗ A
2. ✓ B
3. ✗ C
4. ✗ D

Question Number : 8 Question Type : NAT

Fill in the missing value



Correct Answer :

3

Question Number : 9 Question Type : MCQ

A cube of side 3 units is formed using a set of smaller cubes of side 1 unit. Find the proportion of the number of faces of the smaller cubes visible to those which are NOT visible.

- (A) 1 : 4 (B) 1 : 3 (C) 1 : 2 (D) 2 : 3

Options :

1. ✖ A
2. ✖ B
3. ✔ C
4. ✖ D

Question Number : 10 Question Type : MCQ

Humpty Dumpty sits on a wall every day while having lunch. The wall sometimes breaks. A person sitting on the wall falls if the wall breaks.

Which one of the statements below is logically valid and can be inferred from the above sentences?

- (A) Humpty Dumpty always falls while having lunch
(B) Humpty Dumpty does not fall sometimes while having lunch
(C) Humpty Dumpty never falls during dinner
(D) When Humpty Dumpty does not sit on the wall, the wall does not break

Options :

1. ✖ A
2. ✔ B
3. ✖ C
4. ✖ D

Electronics and Communication Engineering

Number of Questions:

55

Section Marks:

85.0

Q.11 to Q.35 carry 1 mark each & Q.36 to Q.65 carry 2 marks each.

Question Number : 11 Question Type : NAT

Consider a system of linear equations:

$$\begin{aligned}x - 2y + 3z &= -1, \\x - 3y + 4z &= 1, \text{ and} \\-2x + 4y - 6z &= k.\end{aligned}$$

The value of k for which the system has infinitely many solutions is _____.

Correct Answer:

2

Question Number : 12 Question Type : MCQ



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A function $f(x) = 1 - x^2 + x^3$ is defined in the closed interval $[-1, 1]$. The value of x , in the open interval $(-1, 1)$ for which the mean value theorem is satisfied, is

- (A) $-1/2$ (B) $-1/3$ (C) $1/3$ (D) $1/2$

Options :

1. ✖ A
2. ✔ B
3. ✖ C
4. ✖ D

Question Number : 13 Question Type : MCQ

Suppose A and B are two independent events with probabilities $P(A) \neq 0$ and $P(B) \neq 0$. Let $\bar{A}$ and $\bar{B}$ be their complements. Which one of the following statements is FALSE?

- (A) $P(A \cap B) = P(A)P(B)$ (B) $P(A|B) = P(A)$
 (C) $P(A \cup B) = P(A) + P(B)$ (D) $P(\bar{A} \cap \bar{B}) = P(\bar{A})P(\bar{B})$

Options :

1. ✖ A
2. ✖ B
3. ✔ C
4. ✖ D

Question Number : 14 Question Type : MCQ

Let $z = x + iy$ be a complex variable. Consider that contour integration is performed along the unit circle in anticlockwise direction. Which one of the following statements is NOT TRUE?

- (A) The residue of $\frac{z}{z^2 - 1}$ at $z = 1$ is $1/2$
 (B) $\oint_C z^2 dz = 0$
 (C) $\frac{1}{2\pi i} \oint_C \frac{1}{z} dz = 1$
 (D) $\bar{z}$ (complex conjugate of z) is an analytical function

Options :

1. ✖ A
2. ✖ B
3. ✖ C
4. ✔ D

Question Number : 15 Question Type : NAT

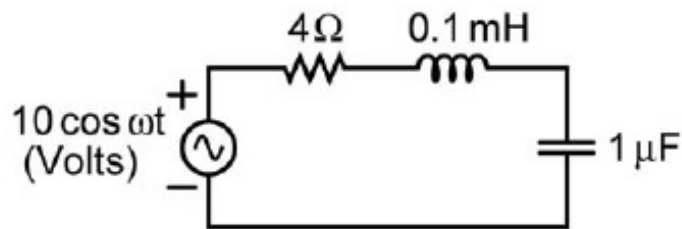
The value of p such that the vector $\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$ is an eigenvector of the matrix $\begin{bmatrix} 4 & 1 & 2 \\ p & 2 & 1 \\ 14 & -4 & 10 \end{bmatrix}$ is _____.

Correct Answer :

16.5 to 17.5

Question Number : 16 Question Type : NAT

In the circuit shown, at resonance, the amplitude of the sinusoidal voltage (in Volts) across the capacitor is _____.

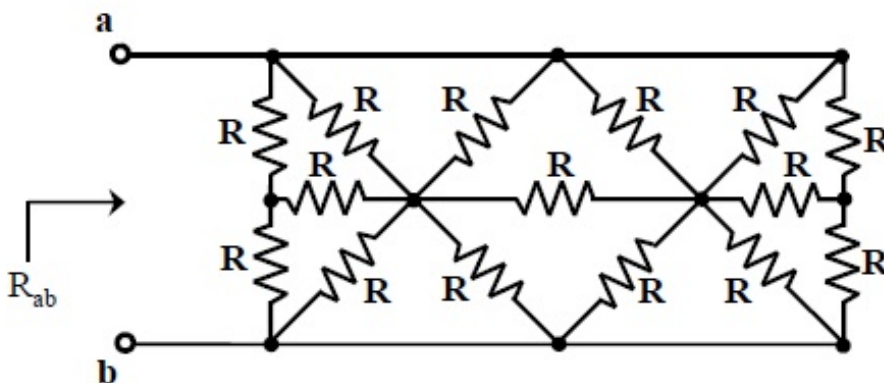


Correct Answer:

24 to 26

Question Number : 17 Question Type : NAT

In the network shown in the figure, all resistors are identical with $R = 300 \Omega$. The resistance R_{ab} (in Ω) of the network is _____.



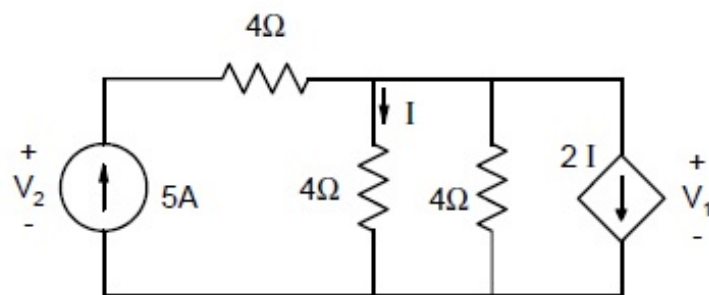
$R = 300 \Omega$

Correct Answer :

99.5 to 100.5

Question Number : 18 Question Type : MCQ

In the given circuit, the values of V_1 and V_2 respectively are



- (A) 5 V, 25 V (B) 10 V, 30 V (C) 15 V, 35 V (D) 0 V, 20 V

Options :

1. ✓ A
2. ✗ B
3. ✗ C
4. ✗ D

Question Number : 19 Question Type : MCQ

A region of negative differential resistance is observed in the current voltage characteristics of a silicon PN junction if

- (A) both the P-region and the N-region are heavily doped
(B) the N-region is heavily doped compared to the P-region
(C) the P-region is heavily doped compared to the N-region
(D) an intrinsic silicon region is inserted between the P-region and the N-region

Options :

1. ✓ A
2. ✗ B
3. ✗ C
4. ✗ D

Question Number : 20 Question Type : NAT

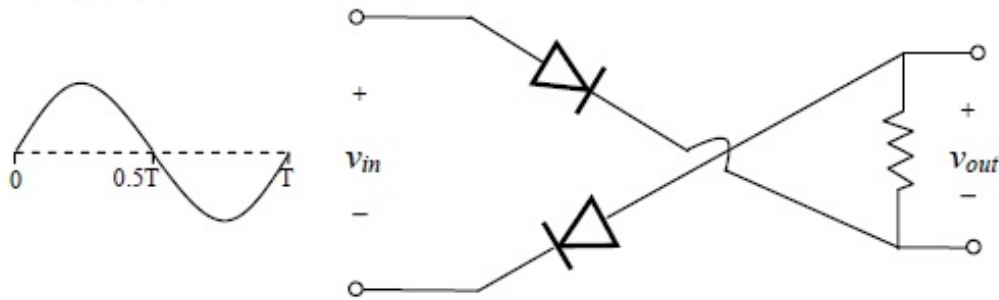
A silicon sample is uniformly doped with donor type impurities with a concentration of $10^{16}/\text{cm}^3$. The electron and hole mobilities in the sample are $1200 \text{ cm}^2/\text{V-s}$ and $400 \text{ cm}^2/\text{V-s}$ respectively. Assume complete ionization of impurities. The charge of an electron is $1.6 \times 10^{-19} \text{ C}$. The resistivity of the sample (in $\Omega\text{-cm}$) is _____.

Correct Answer :

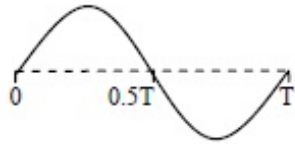
0.50 to 0.54

Question Number : 21 Question Type : MCQ

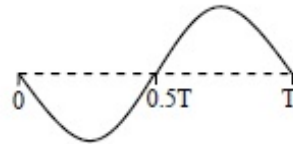
For the circuit with ideal diodes shown in the figure, the shape of the output (v_{out}) for the given sine wave input (v_{in}) will be



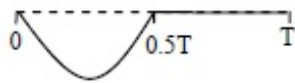
(A)



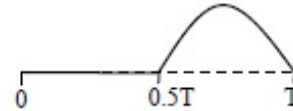
(B)



(C)



(D)

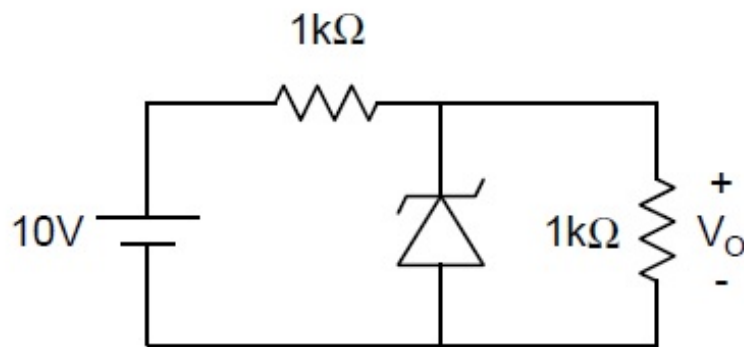


Options :

1. ✖ A
2. ✖ B
3. ✔ C
4. ✖ D

Question Number : 22 Question Type : NAT

In the circuit shown below, the Zener diode is ideal and the Zener voltage is 6 V. The output voltage V_o (in volts) is _____.

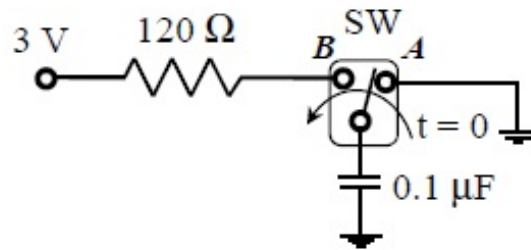


Correct Answer :

5

Question Number : 23 Question Type : MCQ

In the circuit shown, the switch SW is thrown from position *A* to position *B* at time $t = 0$. The energy (in μJ) taken from the 3 V source to charge the $0.1\ \mu\text{F}$ capacitor from 0 V to 3 V is



- (A) 0.3 (B) 0.45 (C) 0.9 (D) 3

Options :

1. ✗ A
2. ✗ B
3. ✓ C
4. ✗ D

Question Number : 24 Question Type : MCQ

In an 8085 microprocessor, the shift registers which store the result of an addition and the overflow bit are, respectively

- (A) B and F
(B) A and F
(C) H and F
(D) A and C

Options :

1. ✗ A
2. ✓ B
3. ✗ C
4. ✗ D

Question Number : 25 Question Type : NAT

A 16 Kb (=16,384 bit) memory array is designed as a square with an aspect ratio of one (number of rows is equal to the number of columns). The minimum number of address lines needed for the row decoder is _____.

Correct Answer:

7

Question Number : 26 Question Type : NAT

Consider a four bit D to A converter. The analog value corresponding to digital signals of values 0000 and 0001 are 0 V and 0.0625 V respectively. The analog value (in Volts) corresponding to the digital signal 1111 is _____.

Correct Answer :

0.93 to 0.94

Question Number : 27 Question Type : MCQ

The result of the convolution $x(-t) * \delta(-t - t_0)$ is

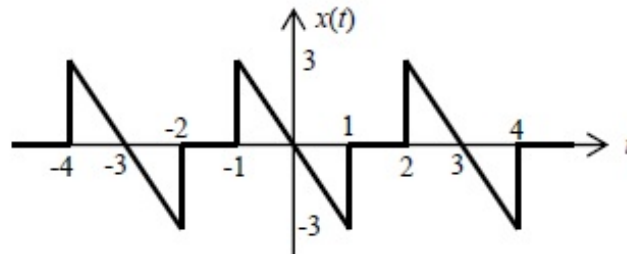
- (A) $x(t + t_0)$ (B) $x(t - t_0)$ (C) $x(-t + t_0)$ (D) $x(-t - t_0)$

Options :

1. ✗ A
2. ✗ B
3. ✗ C
4. ✓ D

Question Number : 28 Question Type : NAT

The waveform of a periodic signal $x(t)$ is shown in the figure.



A signal $g(t)$ is defined by $g(t) = x\left(\frac{t-1}{2}\right)$. The average power of $g(t)$ is _____.

Correct Answer :

2

Question Number : 29 Question Type : MCQ

Negative feedback in a closed-loop control system **DOES NOT**

- (A) reduce the overall gain (B) reduce bandwidth
(C) improve disturbance rejection (D) reduce sensitivity to parameter variation

Options :

1. ✗ A
2. ✓ B



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3. ✖ C

4. ✖ D

Question Number : 30 Question Type : NAT

A unity negative feedback system has the open-loop transfer function $G(s) = \frac{K}{s(s+1)(s+3)}$. The value of the gain K (>0) at which the root locus crosses the imaginary axis is _____.

Correct Answer :

12

Question Number : 31 Question Type : MCQ

The polar plot of the transfer function $G(s) = \frac{10(s+1)}{s+10}$ for $0 \leq \omega < \infty$ will be in the

- (A) first quadrant
- (B) second quadrant
- (C) third quadrant
- (D) fourth quadrant

Options :

1. ✔ A

2. ✖ B

3. ✖ C

4. ✖ D

Question Number : 32 Question Type : MCQ

A sinusoidal signal of 2 kHz frequency is applied to a delta modulator. The sampling rate and step-size Δ of the delta modulator are 20,000 samples per second and 0.1 V, respectively. To prevent slope overload, the maximum amplitude of the sinusoidal signal (in Volts) is

- | | |
|----------------------|---------------------|
| (A) $\frac{1}{2\pi}$ | (B) $\frac{1}{\pi}$ |
| (C) $\frac{2}{\pi}$ | (D) π |

Options :

1. ✔ A

2. ✖ B

3. ✖ C

4. ✖ D

Question Number : 33 Question Type : MCQ

Consider the signal $s(t) = m(t) \cos(2\pi f_c t) + \hat{m}(t) \sin(2\pi f_c t)$ where $\hat{m}(t)$ denotes the Hilbert transform of $m(t)$ and the bandwidth of $m(t)$ is very small compared to f_c . The signal $s(t)$ is a

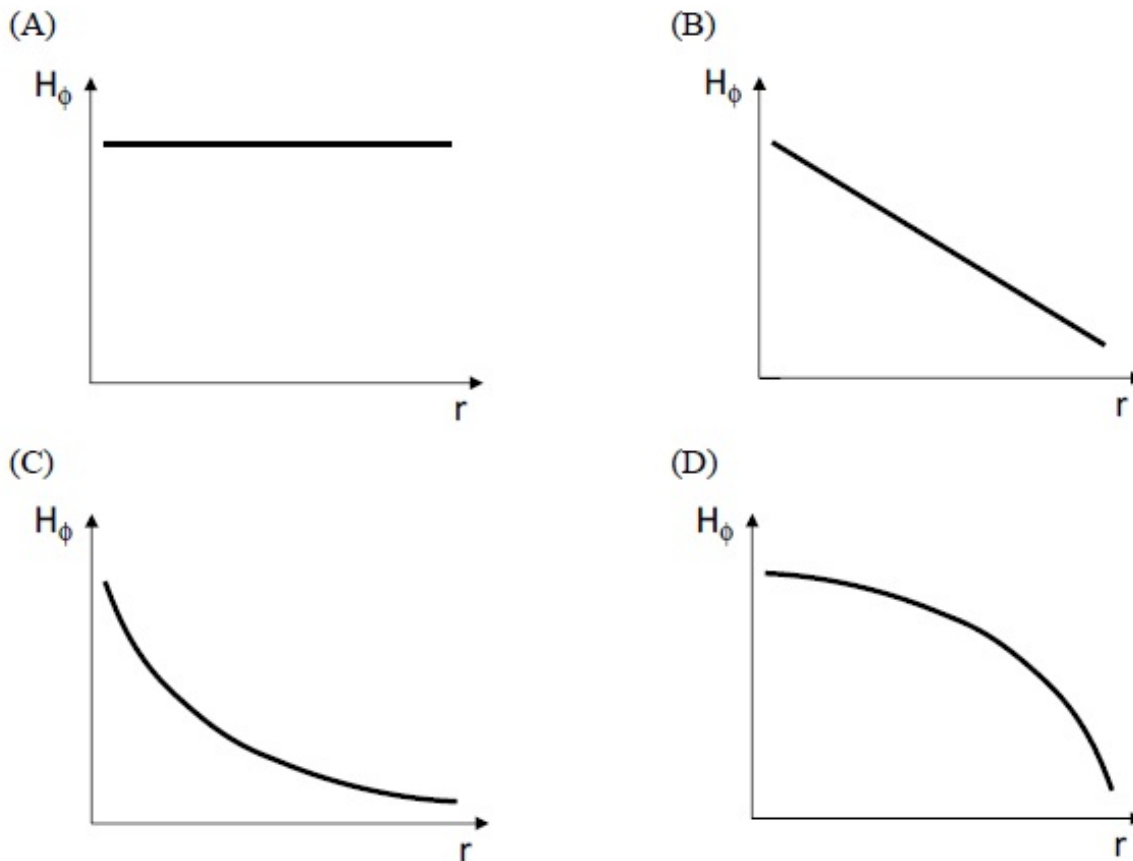
- (A) high-pass signal
- (B) low-pass signal
- (C) band-pass signal
- (D) double sideband suppressed carrier signal

Options :

- 1. ✗ A
- 2. ✗ B
- 3. ✓ C
- 4. ✗ D

Question Number : 34 Question Type : MCQ

Consider a straight, infinitely long, current carrying conductor lying on the z -axis. Which one of the following plots (in linear scale) qualitatively represents the dependence of H_ϕ on r , where H_ϕ is the magnitude of the azimuthal component of magnetic field outside the conductor and r is the radial distance from the conductor?



Options :

- 1. ✗ A
- 2. ✗ B
- 3. ✓ C
- 4. ✗ D

Question Number : 35 Question Type : NAT



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The electric field component of a plane wave traveling in a lossless dielectric medium is given by

$\vec{E}(z,t) = \hat{a}_y 2 \cos\left(10^8 t - \frac{z}{\sqrt{2}}\right)$ V/m. The wavelength (in m) for the wave is _____.

Correct Answer :

8.85 to 8.92

Question Number : 36 Question Type : MCQ

The solution of the differential equation $\frac{d^2 y}{dt^2} + 2 \frac{dy}{dt} + y = 0$ with $y(0) = y'(0) = 1$ is

- (A) $(2-t)e^t$ (B) $(1+2t)e^{-t}$
(C) $(2+t)e^{-t}$ (D) $(1-2t)e^t$

Options :

1. ✖ A
2. ✔ B
3. ✖ C
4. ✖ D

Question Number : 37 Question Type : MCQ

A vector $\vec{P}$ is given by $\vec{P} = x^3 y \vec{a}_x - x^2 y^2 \vec{a}_y - x^2 y z \vec{a}_z$. Which one of the following statements is TRUE?

- (A) $\vec{P}$ is solenoidal, but not irrotational
(B) $\vec{P}$ is irrotational, but not solenoidal
(C) $\vec{P}$ is neither solenoidal nor irrotational
(D) $\vec{P}$ is both solenoidal and irrotational

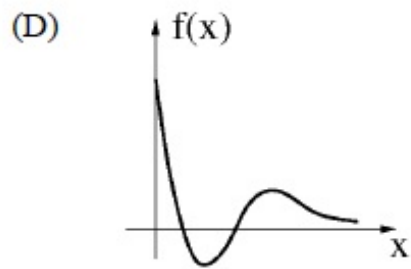
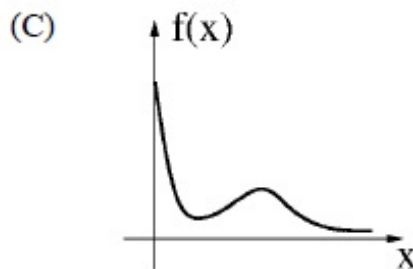
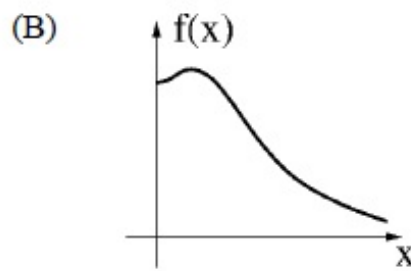
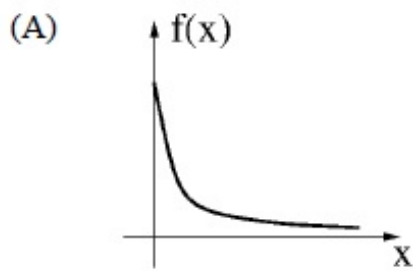
Options :

1. ✔ A
2. ✖ B
3. ✖ C
4. ✖ D

Question Number : 38 Question Type : MCQ



Which one of the following graphs describes the function $f(x) = e^{-x}(x^2 + x + 1)$?



Options :

1. ✗ A
2. ✓ B
3. ✗ C
4. ✗ D

Question Number : 39 Question Type : NAT

The maximum area (in square units) of a rectangle whose vertices lie on the ellipse $x^2 + 4y^2 = 1$ is _____.

Correct Answer:

0.95 to 1.05

Question Number : 40 Question Type : MCQ

The damping ratio of a series RLC circuit can be expressed as

- (A) $\frac{R^2 C}{2L}$ (B) $\frac{2L}{R^2 C}$ (C) $\frac{R}{2} \sqrt{\frac{C}{L}}$ (D) $\frac{2}{R} \sqrt{\frac{L}{C}}$

Options :

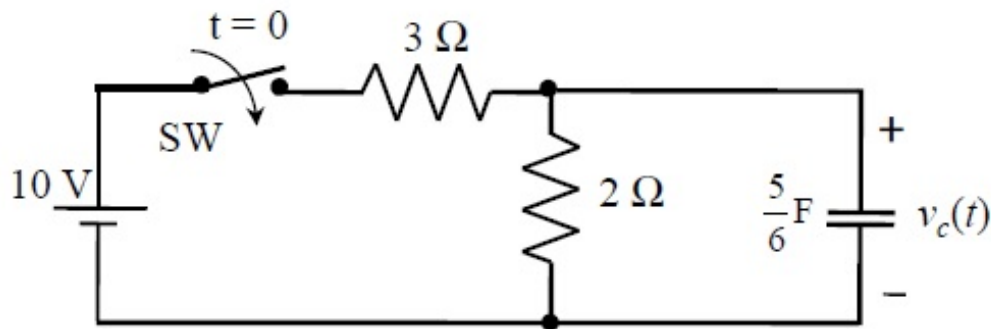
1. ✗ A
2. ✗ B
3. ✓ C
4. ✗ D

Question Number : 41 Question Type : NAT



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In the circuit shown, switch SW is closed at $t = 0$. Assuming zero initial conditions, the value of $v_c(t)$ (in Volts) at $t = 1$ sec is _____.

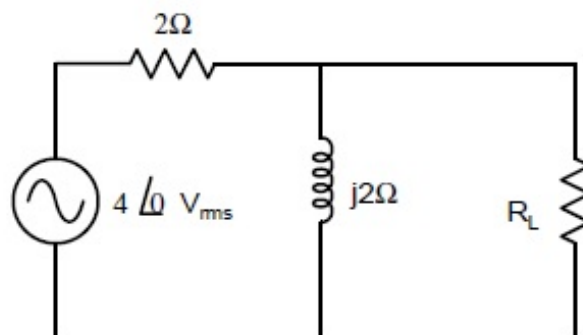


Correct Answer:

2.48 to 2.58

Question Number : 42 Question Type : NAT

In the given circuit, the maximum power (in Watts) that can be transferred to the load R_L is _____.



Correct Answer:

1.6 to 1.7

Question Number : 43 Question Type : NAT

The built-in potential of an abrupt p-n junction is 0.75 V. If its junction capacitance (C_J) at a reverse bias (V_R) of 1.25 V is 5 pF, the value of C_J (in pF) when $V_R = 7.25$ V is _____.

Correct Answer :

2.4 to 2.6

Question Number : 44 Question Type : NAT



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A MOSFET in saturation has a drain current of 1 mA for $V_{DS} = 0.5$ V. If the channel length modulation coefficient is 0.05 V^{-1} , the output resistance (in $k\Omega$) of the MOSFET is _____.

Correct Answer :

19 to 21

Question Number : 45 Question Type : NAT

For a silicon diode with long P and N regions, the acceptor and donor impurity concentrations are $1 \times 10^{17} \text{ cm}^{-3}$ and $1 \times 10^{15} \text{ cm}^{-3}$, respectively. The lifetimes of electrons in P region and holes in N region are both 100 μs . The electron and hole diffusion coefficients are $49 \text{ cm}^2/\text{s}$ and $36 \text{ cm}^2/\text{s}$, respectively. Assume $kT/q = 26 \text{ mV}$, the intrinsic carrier concentration is $1 \times 10^{10} \text{ cm}^{-3}$, and $q = 1.6 \times 10^{-19} \text{ C}$. When a forward voltage of 208 mV is applied across the diode, the hole current density (in nA/cm^2) injected from P region to N region is _____.

Correct Answer :

28 to 30

Question Number : 46 Question Type : MCQ

The Boolean expression $F(X,Y,Z) = \bar{X}Y\bar{Z} + X\bar{Y}\bar{Z} + XY\bar{Z} + XYZ$ converted into the canonical product of sum (POS) form is

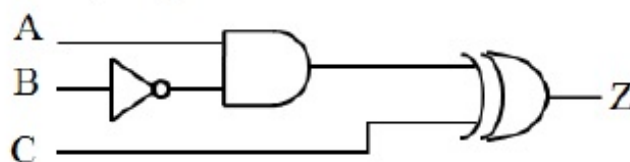
- (A) $(X+Y+Z)(X+Y+\bar{Z})(X+\bar{Y}+\bar{Z})(\bar{X}+Y+\bar{Z})$ (B) $(X+\bar{Y}+Z)(\bar{X}+Y+\bar{Z})(\bar{X}+\bar{Y}+Z)(\bar{X}+\bar{Y}+\bar{Z})$
 (C) $(X+Y+Z)(\bar{X}+Y+\bar{Z})(X+\bar{Y}+Z)(\bar{X}+\bar{Y}+\bar{Z})$ (D) $(X+\bar{Y}+\bar{Z})(\bar{X}+Y+Z)(\bar{X}+\bar{Y}+Z)(X+Y+Z)$

Options :

1. ✓ A
2. ✗ B
3. ✗ C
4. ✗ D

Question Number : 47 Question Type : NAT

All the logic gates shown in the figure have a propagation delay of 20 ns. Let $A = C = 0$ and $B = 1$ until time $t = 0$. At $t = 0$, all the inputs flip (i.e., $A = C = 1$ and $B = 0$) and remain in that state. For $t > 0$, output $Z = 1$ for a duration (in ns) of _____.



Correct Answer :

40



Question Number : 48 Question Type : MCQ

A 3-input majority gate is defined by the logic function $M(a,b,c) = ab + bc + ca$. Which one of the following gates is represented by the function $M(\overline{M(a,b,c)}, M(a,b,\overline{c}), c)$?

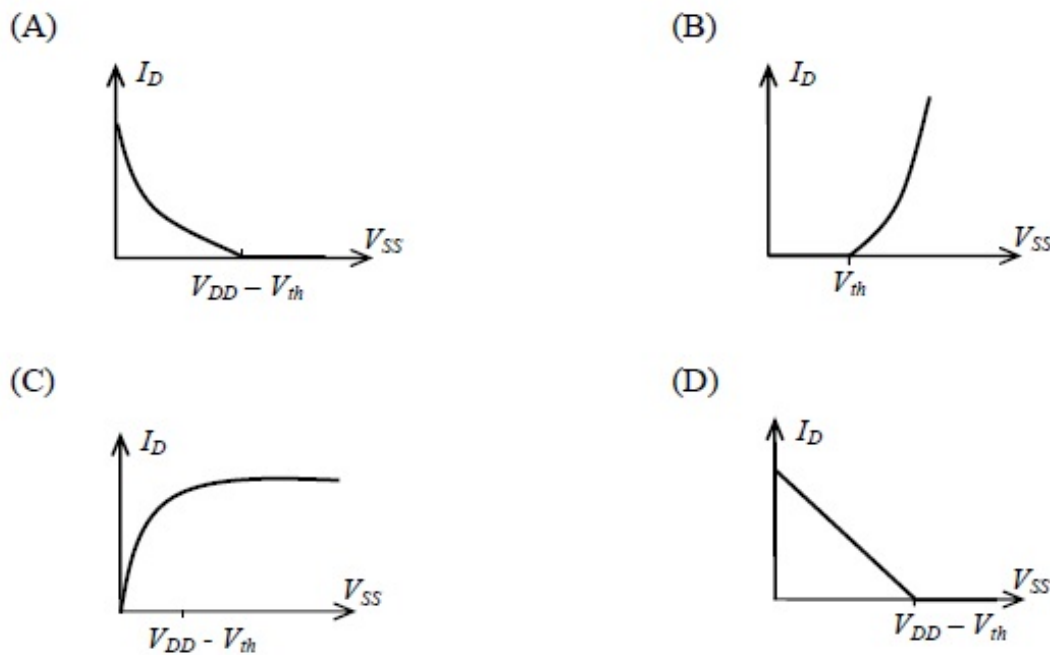
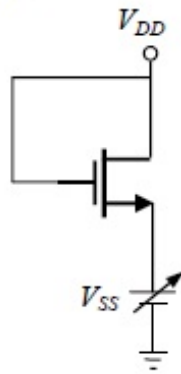
- (A) 3-input NAND gate
- (B) 3-input XOR gate
- (C) 3-input NOR gate
- (D) 3-input XNOR gate

Options :

- 1. ✗ A
- 2. ✓ B
- 3. ✗ C
- 4. ✗ D

Question Number : 49 Question Type : MCQ

For the NMOSFET in the circuit shown, the threshold voltage is V_{th} , where $V_{th} > 0$. The source voltage V_{SS} is varied from 0 to V_{DD} . Neglecting the channel length modulation, the drain current I_D as a function of V_{SS} is represented by



Options :

- 1. ✓ A
- 2. ✗ B
- 3. ✗ C
- 4. ✗ D

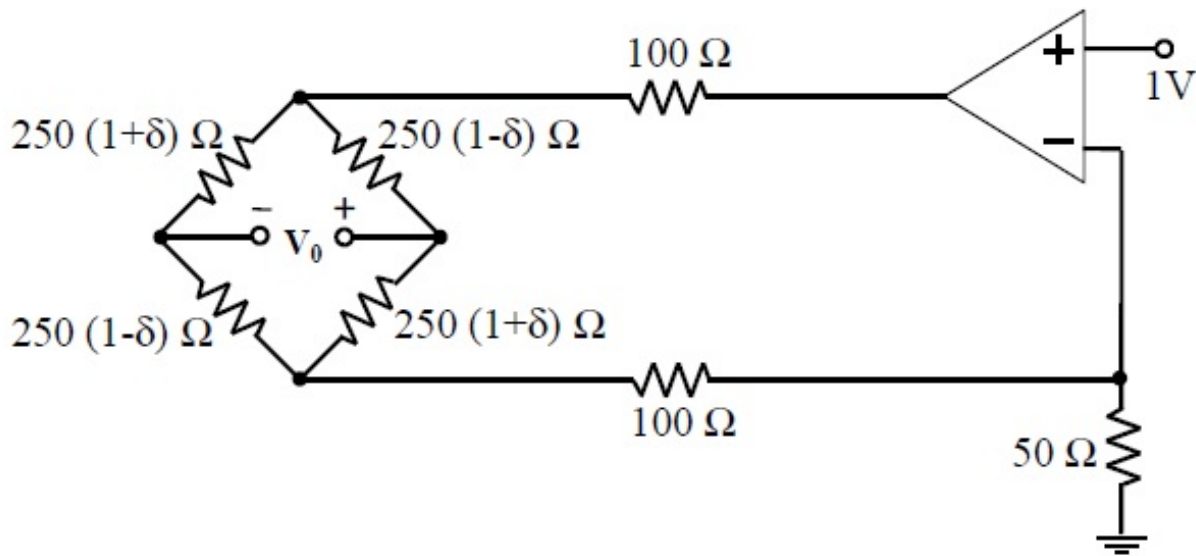


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Question Number : 50 Question Type : NAT

In the circuit shown, assume that the opamp is ideal. The bridge output voltage V_0 (in mV) for $\delta = 0.05$ is _____.

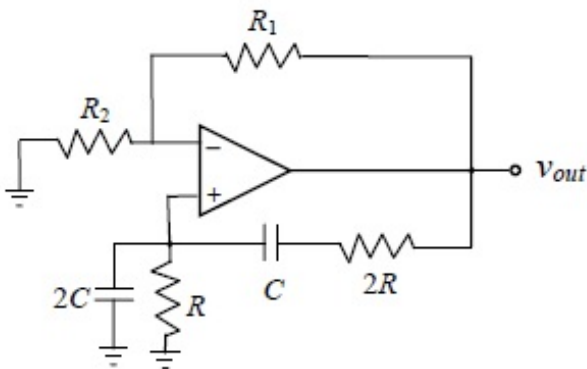


Correct Answer :

249 to 251

Question Number : 51 Question Type : MCQ

The circuit shown in the figure has an ideal opamp. The oscillation frequency and the condition to sustain the oscillations, respectively, are



- (A) $\frac{1}{CR}$ and $R_1 = R_2$
 (C) $\frac{1}{2CR}$ and $R_1 = R_2$

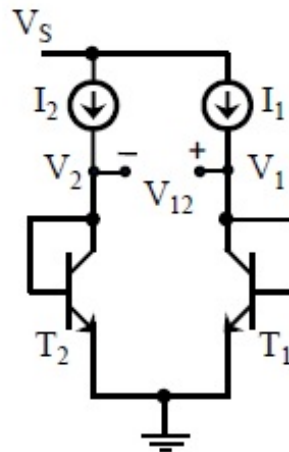
- (B) $\frac{1}{CR}$ and $R_1 = 4R_2$
 (D) $\frac{1}{2CR}$ and $R_1 = 4R_2$

Options :

1. ✗ A
2. ✗ B
3. ✗ C
4. ✓ D



In the circuit shown, $I_1 = 80 \text{ mA}$ and $I_2 = 4 \text{ mA}$. Transistors T_1 and T_2 are identical. Assume that the thermal voltage V_T is 26 mV at 27°C . At 50°C , the value of the voltage $V_{12} = V_1 - V_2$ (in mV) is _____.



Correct Answer :

83.5 to 84.0

Question Number : 53 Question Type : MCQ

Two sequences $[a, b, c]$ and $[A, B, C]$ are related as,

$$\begin{bmatrix} A \\ B \\ C \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & W_3^{-1} & W_3^{-2} \\ 1 & W_3^{-2} & W_3^{-4} \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} \quad \text{where } W_3 = e^{j\frac{2\pi}{3}}.$$

If another sequence $[p, q, r]$ is derived as,

$$\begin{bmatrix} p \\ q \\ r \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & W_3^1 & W_3^2 \\ 1 & W_3^2 & W_3^4 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & W_3^2 & 0 \\ 0 & 0 & W_3^4 \end{bmatrix} \begin{bmatrix} A/3 \\ B/3 \\ C/3 \end{bmatrix},$$

then the relationship between the sequences $[p, q, r]$ and $[a, b, c]$ is

- (A) $[p, q, r] = [b, a, c]$ (B) $[p, q, r] = [b, c, a]$
 (C) $[p, q, r] = [c, a, b]$ (D) $[p, q, r] = [c, b, a]$

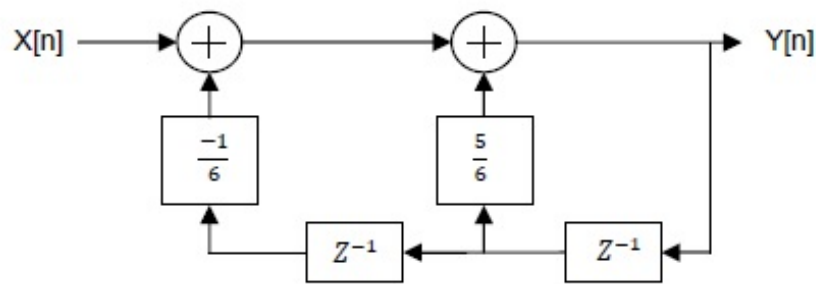
Options :

1. ✗ A
 2. ✗ B
 3. ✓ C
 4. ✗ D

Question Number : 54 Question Type : MCQ



For the discrete-time system shown in the figure, the poles of the system transfer function are located at



(A) 2, 3

(B) $\frac{1}{2}$, 3

(C) $\frac{1}{2}$, $\frac{1}{3}$

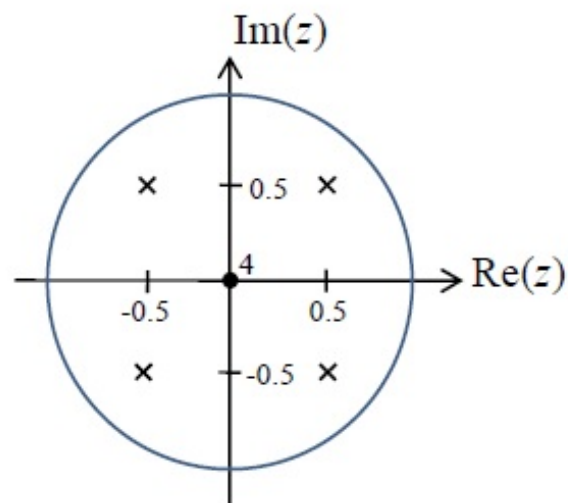
(D) 2, $\frac{1}{3}$

Options :

1. ✗ A
2. ✗ B
3. ✓ C
4. ✗ D

Question Number : 55 Question Type : MCQ

The pole-zero diagram of a causal and stable discrete-time system is shown in the figure. The zero at the origin has multiplicity 4. The impulse response of the system is $h[n]$. If $h[0] = 1$, we can conclude



- (A) $h[n]$ is real for all n
- (B) $h[n]$ is purely imaginary for all n
- (C) $h[n]$ is real for only even n
- (D) $h[n]$ is purely imaginary for only odd n

Options :

1. ✓ A
2. ✗ B
3. ✗ C
4. ✗ D

Question Number : 56 Question Type : NAT



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The open-loop transfer function of a plant in a unity feedback configuration is given as

$G(s) = \frac{K(s+4)}{(s+8)(s^2-9)}$. The value of the gain $K(>0)$ for which $-1+j2$ lies on the root locus is _____.

Correct Answer :

25 to 26

Question Number : 57 Question Type : NAT

A lead compensator network includes a parallel combination of R and C in the feed-forward path. If

the transfer function of the compensator is $G_c(s) = \frac{s+2}{s+4}$, the value of RC is _____.

Correct Answer :

0.5

Question Number : 58 Question Type : MCQ

A plant transfer function is given as $G(s) = \left(K_p + \frac{K_I}{s} \right) \frac{1}{s(s+2)}$. When the plant operates in a unity feedback configuration, the condition for the stability of the closed loop system is

(A) $K_p > \frac{K_I}{2} > 0$ (B) $2K_I > K_p > 0$ (C) $2K_I < K_p$ (D) $2K_I > K_p$

Options :

1. ✓ A

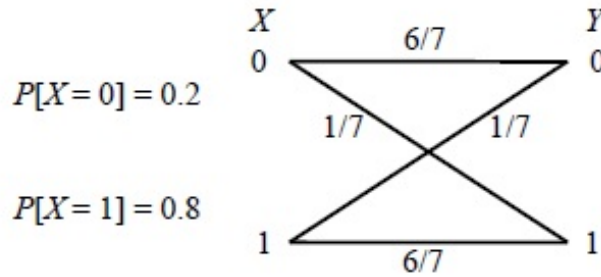
2. ✗ B

3. ✗ C

4. ✗ D

Question Number : 59 Question Type : NAT

The input X to the Binary Symmetric Channel (BSC) shown in the figure is '1' with probability 0.8. The cross-over probability is $1/7$. If the received bit $Y = 0$, the conditional probability that '1' was transmitted is _____.



Correct Answer :

0.39 to 0.41

Question Number : 60 Question Type : NAT

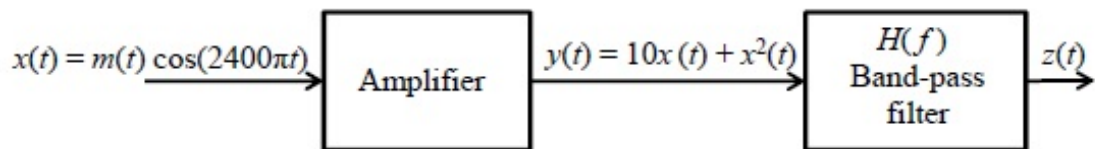
The transmitted signal in a GSM system is of 200 kHz bandwidth and 8 users share a common bandwidth using TDMA. If at a given time 12 users are talking in a cell, the total bandwidth of the signal received by the base station of the cell will be at least (in kHz) _____.

Correct Answer:

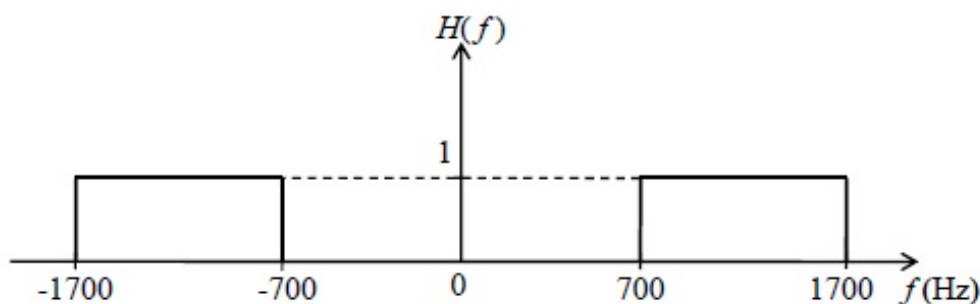
400

Question Number : 61 Question Type : NAT

In the system shown in Figure (a), $m(t)$ is a low-pass signal with bandwidth W Hz. The frequency response of the band-pass filter $H(f)$ is shown in Figure (b). If it is desired that the output signal $z(t) = 10x(t)$, the maximum value of W (in Hz) should be strictly less than _____.



(a)



(b)



Correct Answer :

349 to 350

Question Number : 62 Question Type : MCQ

A source emits bit 0 with probability $\frac{1}{3}$ and bit 1 with probability $\frac{2}{3}$. The emitted bits are communicated to the receiver. The receiver decides for either 0 or 1 based on the received value R . It is given that the conditional density functions of R are as

$$f_{R|0}(r) = \begin{cases} \frac{1}{4}, & -3 \leq x \leq 1, \\ 0, & \text{otherwise,} \end{cases} \quad \text{and} \quad f_{R|1}(r) = \begin{cases} \frac{1}{6}, & -1 \leq x \leq 5, \\ 0, & \text{otherwise.} \end{cases}$$

The minimum decision error probability is

- (A) 0 (B) 1/12 (C) 1/9 (D) 1/6

Options :

1. ✖ A
2. ✖ B
3. ✖ C
4. ✔ D

Question Number : 63 Question Type : MCQ

The longitudinal component of the magnetic field inside an air-filled rectangular waveguide made of a perfect electric conductor is given by the following expression

$$H_z(x, y, z, t) = 0.1 \cos(25\pi x) \cos(30.3\pi y) \cos(12\pi \times 10^9 t - \beta z) \text{ (A/m)}$$

The cross-sectional dimensions of the waveguide are given as $a = 0.08 \text{ m}$ and $b = 0.033 \text{ m}$. The mode of propagation inside the waveguide is

- (A) TM_{12} (B) TM_{21}
(C) TE_{21} (D) TE_{12}

Options :

1. ✖ A
2. ✖ B
3. ✔ C
4. ✖ D

Question Number : 64 Question Type : NAT



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The electric field intensity of a plane wave traveling in free space is given by the following expression

$$\mathbf{E}(x, t) = \mathbf{a}_y 24 \pi \cos(\omega t - k_0 x) \text{ (V/m)}$$

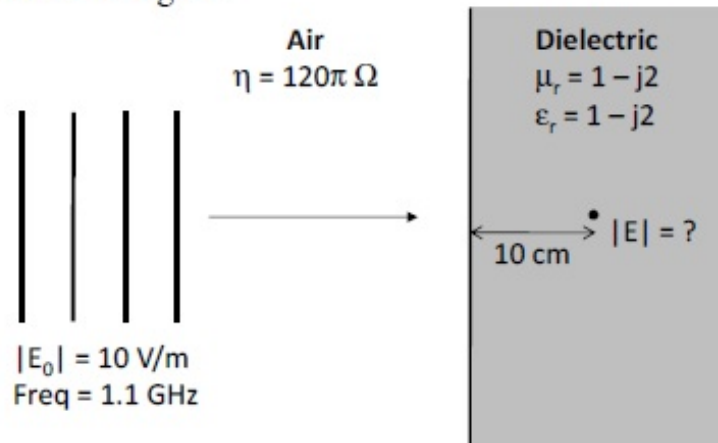
In this field, consider a square area 10 cm x 10 cm on a plane $x + y = 1$. The total time-averaged power (in mW) passing through the square area is _____.

Correct Answer :

53 to 54

Question Number : 65 Question Type : NAT

Consider a uniform plane wave with amplitude (E_0) of 10 V/m and 1.1 GHz frequency travelling in air, and incident normally on a dielectric medium with complex relative permittivity (ϵ_r) and permeability (μ_r) as shown in the figure.



The magnitude of the transmitted electric field component (in V/m) after it has travelled a distance of 10 cm inside the dielectric region is _____.

Correct Answer :

0.08 to 0.12